HIGH SCHOOL GEOMETRY ENRICHMENT PACKET

Tinkham Ed. Center Geometry I Review

Name_____

Circle each correct answer. Show your work!

Question 1



Trigonometric area formula: Area = $\frac{\frac{1}{2}absin(C)}{2}$

What is the area of triangle PQR? Round to the nearest tenth of a square unit.



111.3 square units

- C 185.4 square units
- C 222.5 square units

Question 2

Triangle ABC is a sketch of a triangular flower bed that has an area of 65.1 square feet.



To the nearest foot, what amount of fencing is needed to surround the perimeter of the flower bed?

C 17 feet



C 50 feet

Question 3



- C 364 square units
- C 728 square units

Question 4

A kite is made up of two isosceles triangles, KIT and KET, with the lengths shown. The top triangle of the kite, Δ KIT, is made from approximately 17 square inches of material.



How much material is used for the entire kite, quadrilateral KITE? Round to the nearest square inch.

- 0 31 square inches 0 34 square inches 48 square inches
- C 62 square inches

The law of cosines for \triangle RST can be set up as $5^2 = 7^2 + 3^2 - 2(7)(3)\cos(S)$. What could be true about \triangle RST?

Law of cosines: $a^2 = b^2 + c^2 - 2bc\cos(A)$

 \bigcirc *r* = 5 and *t* = 7

 \bigcirc r = 3 and t = 3 \mathbf{O}

s = 7 and t = 5s = 5 and t = 3

Question 6



Law of cosines: $a^2 = b^2 + c^2 - 2bc\cos(A)$

Which equation correctly uses the law of cosines to solve for y?

C
$$9^2 = y^2 + 19^2 - 2(y)(19)\cos(41^\circ)$$

C $y^2 = 9^2 + 19^2 - 2(y)(19)\cos(41^\circ)$
C $9^2 = y^2 + 19^2 - 2(9)(19)\cos(41^\circ)$
 $y^2 = 9^2 + 19^2 - 2(9)(19)\cos(41^\circ)$







Law of cosines: $a^2 = b^2 + c^2 - 2bc\cos(A)$

Find the measure of $\angle Q$, the smallest angle in a triangle whose sides have lengths 4, 5, and 6. Round the measure to the nearest whole degree.





 \Box *m*∠K = 94°

 $k \approx 3.7$ units

 $k \approx 4.6$ units

 \Box

 \Box

KL ≈ 2.5 units

KL ≈ 3.2 units

Question 10

 $\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$ Law of sines:

Triangle ABC has measures a = 2, b = 2, and $m \perp A = 30^{\circ}$. What is the measure of angle B?

0 15° 30° O 45° \bigcirc 60°

Question 11

 $\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$ Law of sines:

In \triangle BCD, d = 3, b = 5, and $m \angle D = 25^{\circ}$. What are the possible approximate measures of angle B?

О only 90°

 \bigcirc

only 155°

20° and 110° 45° and 135°

Question 12

Two teams are pulling a heavy chest, located at point X. The teams are 4.6 meters away from each other. Team A is 2.4 meters away from the chest, and Team B is 3.2 meters away. Their ropes are attached at an angle of 110°.



Law of sines: $a = \frac{b}{b}$

Which equation can be used to solve for angle A?

С

$$\frac{\sin (A)}{2.4} = \frac{\sin (110^{\circ})}{4.6}$$

$$\frac{\sin (A)}{4.6} = \frac{\sin (110^{\circ})}{2.4}$$

$$\frac{\sin (A)}{3.2} = \frac{\sin (110^{\circ})}{4.6}$$

$$\frac{\sin (A)}{4.6} = \frac{\sin (110^{\circ})}{3.2}$$

Question 13



Which equation can be used to find the measure of angle LJK?

 \bigcirc

$$\begin{array}{c} C \\ \sin(x) = \frac{10}{15} \\ \frac{15}{10} \\ \sin(x) = \frac{10}{10} \\ \cos(x) = \frac{10}{15} \\ C \\ \cos(x) = \frac{15}{10} \end{array}$$

In which triangle is the value of x equal to $\tan^{-1} \left(\frac{3.1}{5.2}\right)$?

(Images may not be drawn to scale.)



Question 15



What is the measure of angle LKJ? Round to the nearest whole degree.



Question 16

In right triangle XYZ, the right angle is located at vertex Y. The length of line segment XY is 12.4 cm. The length of line segment YZ is 15.1 cm.

Which is the approximate measure of angle YZX?



C 55.2°

Question 17

Which equation can be used to find the length of \overline{AC} ?



Triangle ABC is a right triangle and $cos(22.6) = \frac{b}{13}$. Solve for *b* and round to the nearest whole number.



Which equation correctly uses the value of *b* to solve for *a*?

C $\tan(22.6^{\circ}) = \frac{13}{13}$ C $\tan(22.6^{\circ}) = \frac{a}{12}$ $\tan(22.6^{\circ}) = \frac{12}{12}$ C $\tan(22.6^{\circ}) = \frac{12}{a}$

Question 19

 $sin(25^\circ) = \frac{9}{c}$ can be used to find the length of \overline{AB} .



What is the length of \overline{AB} ? Round to the nearest tenth.

C 19.3 in. 21.3 in.





Question 20

A right triangle has one angle that measure 23°. The adjacent leg measures 27.6 cm and the hypotenuse measures 30 cm.

What is the approximate area of the triangle? Round to the nearest tenth.

Area of a triangle =
$$\frac{1}{2}bh$$

68.7 cm²
161.8 cm²
381.3 cm²

O 450.0 cm²

ć

Question 21



Which statements are true about triangle QRS? Select three options.

The side opposite $\angle Q$ is RS.
The side opposite $\angle R$ is RQ.
The hypotenuse is QR.
The side adjacent to $\angle R$ is SQ.
The side adjacent to $\angle Q$ is \overline{QS} .

Objective: Given an acute angle of a right triangle, write ratios for sine, cosine, and tangent.



Given right triangle DEF, what is the value of tan(F)?



Question 23

Objective: Given an acute angle of a right triangle, write ratios for sine, cosine, and tangent.



Given right triangle ABC, what is the value of tan(A)?

 $\begin{array}{c} \frac{5}{13} \\ \frac{12}{13} \\ \frac{12}{13} \\ \frac{12}{5} \\ \frac{13}{12} \\ \end{array}$

Question 24

Objective: Relate trigonometric ratios of similar triangles and the acute angles of a right triangle.

Use the diagram to complete the statement.



Given △JKL, sin(38°) equals

C cos(38°). cos(52°).

C tan(38°).

C tan(52°).

Question 25

Objective: Determine unknown measures of 45°-45°-90° triangles.

The hypotenuse of a 45°-45°-90° triangle measures $22\sqrt{2}$ units.



What is the length of one leg of the triangle?



Question 26 Objective: Determine unknown measures of 45°-45°-90° triangles.



The hypotenuse of a 45°-45°-90° triangle measures 4 cm. What is the length of one leg of the triangle?



Question 27 Objective: Determine unknown measures of 30°-60°-90° triangles.



What are the angle measures of triangle VUW?

- $m_{\perp}V = 30^{\circ}, m_{\perp}U = 60^{\circ}, m_{\perp}W = 90^{\circ}$
- $m_{\perp}V = 90^{\circ}, m_{\perp}U = 60^{\circ}, m_{\perp}W = 30^{\circ}$
- C $m \ge V = 30^{\circ}, m \ge U = 90^{\circ}, m \ge W = 60^{\circ}$ $m \ge V = 60^{\circ}, m \ge U = 90^{\circ}, m \ge W = 30^{\circ}$

<u>Question 28</u> Objective: Determine unknown measures of 30°-60°-90° triangles.

The diagonal of rectangle ABCD measures 2 inches in length.



What is the length of line segment AB?



 $^{\circ}$ 4 inches $^{\circ}$ $^{4\sqrt{3}}$ inches

Question 29

Objective: Classify a triangle using the converse of the Pythagorean theorem and triangle inequality theorems.

Which classification best represents a triangle with side lengths 10 in., 12 in., and 15 in.?

acute, because 102+122>152

- C acute, because 12²+15²>10²
- O obtuse, because 10²+12²>15²

O obtuse, because 12²+15²>10²

Question 30

Objective: Apply the converse of the Pythagorean theorem and triangle inequality theorems to solve problems.

Joey is building a frame for a sandbox. The sandbox is going to be a quadrilateral that has the lengths shown.



If the diagonal of the sandbox measures 14 feet, which best describes the shape of the sandbox?

C a rectangle, because angle C is a right angle

C a rectangle, because angle C and angle X are congruent a quadrilateral, because angle C and angle X are acute

a quadrilateral, because angle C and angle X are obtuse

Question 31

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Objective: Determine an unknown side length or range of side lengths of a triangle given its classification.

The lengths of two sides of a right triangle are 5 inches and 8 inches. What is the difference between the two possible lengths of the third side of the triangle? Round your answer to the nearest tenth.

C 3.1 inches 3.2 inches

C 10.0 inches

C 15.7 inches

Question 32

Objective: Determine an unknown side length or range of side lengths of a triangle given its classification.

An acute triangle has side lengths 21 cm, x cm, and 2x cm. If 21 is one of the shorter sides of the triangle, what is the greatest possible length of the longest side, rounded to the nearest tenth?

18.8 cm 24.2 cm

O



Objective: Find the coordinates of a point on a directed line segment that partitions the segment into a given ratio.

On a number line, the directed line segment from Q to S has endpoints Q at -14 and S at 2. Point R partitions the directed line segment from Q to S in a 3:5 ratio.

- L

to find the location of point R?

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Which expression correctly uses the formula
$$\left[\frac{m}{m+n}\right](x_2 - x_1) + x_1$$

 $\left[\frac{3}{3+5}\right](2 - (-14)) + (-14)$
 $\left[\frac{3}{3+5}\right](-14 - 2) + 2$
 $\left[\frac{3}{3+5}\right](2 - 14) + 14$

 $\left(\frac{3}{3+5}\right)(-14-2)-2$

Question 34

Objective: Find the coordinates of a point on a directed line segment that partitions the segment into a given ratio.

If point P is $\overline{7}$ of the distance from M to N, what ratio does the point P partition the directed line segment from M to N into?

\mathbf{O} 4:1

- 4:3
- O 4:7
- O 4:10

Question 35

Objective: Find the coordinates of a point on a directed line segment that partitions the segment into a given ratio.



What are the *x*- and *y*- coordinates of point P on the directed line segment from A to B such that P is $\frac{2}{3}$ the length of the line segment from A to B? $x = \left[\frac{m}{m+n}\right](x_2 - x_1) + x_1$ $y = \left[\frac{m}{m+n}\right](y_2 - y_1) + y_1$ C (2, -1) (4, -3) (-1, 2) C (3, -2)

Question 36

Objective: Model and solve real-world problems involving directed line segments.



A treasure map says that a treasure is buried so that it partitions the distance between a rock and a tree in a 5:9 ratio. Marina traced the map onto a coordinate plane to find the exact location of the treasure.

$$x = \left(\frac{m}{m+n}\right)(x_2 - x_1) + x_1$$
$$y = \left(\frac{m}{m+n}\right)(y_2 - y_1) + y_1$$

What are the coordinates of the treasure? If necessary, round the coordinates to the nearest tenth.

Question 37

Objective: Identify similar right triangles formed by an altitude and write a similarity statement.

WY

is an altitude in triangle WXZ.



Question 38

Objective: Identify similar right triangles formed by an altitude and write a similarity statement.



<u>Question 39</u> Objective: Apply the Pythagorean theorem to find side lengths of a right triangle.



units

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Objective: Apply the Pythagorean theorem to find side lengths of a right triangle.



18 units

Question 41

Objective: Solve for unknown measures of similar triangles using the side-splitter theorem and its converse.



Question 42

Objective: Solve for unknown measures of similar triangles using the side-splitter theorem and its converse.



Question 43

Objective: Solve for unknown measures of similar triangles using the triangle mid - segment theorem.



Question 44

Objective: Solve for unknown measures of similar triangles using the triangle mid-segment theorem.



What is the perimeter of ΔWXY ?

- C 11.57 cm
- C 12.22 cm
- C 12.46 cm 14.50 cm

Objective: Identify the sides and angle that can be used to prove triangle similarity using SSS similarity theorem and SAS similarity theorem.



Which statements can be concluded from the diagram and used to prove that the triangles are similar by the SAS similarity theorem?

$$\frac{RS}{VU} = \frac{ST}{UT} \text{ and } \angle S \cong \angle U$$

$$\frac{RS}{VU} = \frac{ST}{UT} = \frac{RT}{VT}$$

$$\frac{RS}{VU} = \frac{TU}{TS} \text{ and } \angle S \cong \angle U$$

$$\frac{RS}{VU} = \frac{TU}{TS} = \frac{RT}{VT}$$

Question 46

Objective: Identify the sides and angle that can be used to prove triangle similarity using SSS similarity theorem and SAS similarity theorem.

Consider $\triangle RST$ and $\triangle RYX$.



If the triangles are similar, which must be true?

0	$\frac{RY}{YS} = \frac{RX}{XT} = \frac{XY}{TS}$	
	RY_RX_XY	
	RS RT TS	
	<u>RY _ RX _ RS</u>	
\mathbf{O}	RS RT RY	
	$\underline{RY} = \underline{RS} = \underline{XY}$	
0	RX RT TS	

Objective: Identify the sides and angle that can be used to prove triangle similarity using SSS similarity theorem and SAS similarity theorem.

Consider the two triangles.



To prove that the triangles are similar by the SAS similarity theorem, it needs to be shown that

© ∠c≅∠c

 $\bigcirc \ \ \angle C \cong \angle G$ $\bigcirc \ \ \frac{AC}{GI} = \frac{HI}{BC}$ $\frac{AC}{GI} = \frac{BC}{HI}$

Question 48

Objective: Identify the sides and angle that can be used to prove triangle similarity using SSS similarity theorem and SAS similarity theorem.

In the diagram, DG = 12, GF = 4, EH = 9, and HF = 3.



To prove that $\triangle DFE \sim \triangle GFH$ by the SAS similarity theorem, it can be stated that $\frac{DF}{GF} = \frac{EF}{HF}$ and

- \bigcirc $\angle DFE$ is 4 times greater than $\angle GFH$.
- C ∠FHG is $\overline{4}$ the measure of ∠FED. ∠DFE is congruent to ∠GFH.
- C ∠FHG is congruent to ∠EFD

Question 49

Objective: Identify the composition of similarity transformations in a mapping of two triangles.



Which transformations could have occurred to map $\triangle ABC$ to $\triangle A"B"C?$

0

a rotation and a reflection

0

a translation and a dilation

a reflection and a dilation a dilation and a rotation

Question 50

Objective: Identify the composition of similarity transformations in a mapping of two triangles.



Why is the information in the diagram enough to determine that $\triangle LMN \sim \triangle PON$ using a rotation about point N and a dilation?

- C because both triangles appear to be equilateral because∠MNL and ∠ONP are congruent angles
- ^C because one pair of congruent corresponding angles is sufficient to determine similar triangles

because both triangles appear to be isosceles, \angle MLN $\cong \angle$ LMN, and \angle NOP $\cong \angle$ OPN

Question 51

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Objective: Identify the composition of similarity transformations in a mapping of two triangles.

Which best explains why all equilateral triangles are similar?

C All equilateral triangles can be mapped onto each other using dilations.

All equilateral triangles can be mapped onto each other using rigid transformations. All equilateral triangles can be mapped onto each other using combinations of dilations and rigid transformations.

^C All equilateral triangles are congruent and therefore similar, with side lengths in a 1:1 ratio.

Question 52

Objective: Complete the steps to prove triangles are similar using the AA similarity theorem.

Read the proof.

Given: AB || DE

Prove: $\triangle ACB \sim \triangle DCE$

D В Е С

We are given $\overrightarrow{AB} \parallel \overrightarrow{DE}$. Because the lines are parallel and segment CB crosses both lines, we can consider segment CB a transversal of the parallel lines. Angles CED and CBA are corresponding angles of transversal \overrightarrow{CB} and are therefore congruent, so $\angle CED \cong \angle CBA$. We can state $\angle C \cong \angle C$ using the reflexive property. Therefore, $\triangle ACB \sim \triangle DCE$ by the:

AA similarity theorem.

- SSS similarity theorem.
- AAS similarity theorem.
- ASA similarity theorem.

Objective: Verify the properties of dilations, including the scale factor and slopes of corresponding line segments.

Parallelogram FGHJ was dilated and translated to form similar parallelogram F'G'H'J'.



What is the scale factor of the dilation?



Question 54

Objective: Verify the properties of dilations, including the scale factor and slopes of corresponding line segments.



Is rectangle EFGH the result of a dilation of rectangle ABCD with a center of dilation at the origin? Why or why not?

4

Yes, because corresponding sides are parallel and have lengths in the ratio $\frac{1}{3}$

Yes, because both figures are rectangles and all rectangles are similar.

No, because the center of dilation is not at (0, 0).

No, because corresponding sides have different slopes.

Question 55

Objective: Find the coordinates of the vertices of an image or pre-image of a dilated polygon given the scale factor.

Triangle TVW is dilated according to the rule

 $D_{o,\frac{3}{4}}(x,y) \rightarrow \left(\frac{3}{4}x, \frac{3}{4}y\right)$ to create

to create the image triangle T'V'W', which is not shown.



What are the coordinates of the endpoints of the segment T'V'?

T'(-3, 6) and V'(0, 3)

C T'(-3, 6) and V'(0, 1)

0

 \bigcirc

C T'(-1, 2) and V'(0, 3)
 C T'(-1, 2) and V'(0, 1)

Question 56

Objective: Find the coordinates of the vertices of an image or pre-image of a dilated polygon given the scale factor.

- (0, -4)
- C (0, -1)
- **C** (0, 0)
- C (0, 4)

Question 57

Objective: Determine the unknown measures of an image or pre-image of a dilated figure given the scale factor.

If an image of a triangle is congruent to the pre-image, what is the scale factor of the dilation?

^{__} 10

<u>Question 58</u> Objective: Calculate and interpret the scale factor for dilations of figures.



Is triangle A'B'C' a dilation of triangle ABC? Explain.

C Yes, it is an enlargement with a scale factor of 3.

Yes, it is an enlargement with a scale factor of ³.
 No, it is not a dilation because the points of the image are not moved away from the center of dilation proportionally.

No, it is not a dilation because the sides of the image are proportionally reduced from the pre-image.

Question 59

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Objective: Determine the unknown measures of an image or pre-image of a dilated figure given the scale factor.



C 20 units

Objective: Determine the unknown measures of an image or pre-image of a dilated figure given the scale factor.

Triangle RST was dilated by a scale factor of $\frac{1}{2}$. The image, triangle R'S'T', is an isosceles triangle, with each leg measuring 8 units.



What is the length of a leg of the pre-image, triangle RST?



C 8 units 16 units

C 20 units

Question 61

Objective: Identify the triangle congruency theorem that can be used to prove two triangles congruent.

Given: \overline{RS} bisects $\angle MRQ$; $\angle RMS \cong \angle RQS$



Which relationship in the diagram is true?

- \bigcirc $\Delta SNQ \cong \Delta SNM$ by SSS

 $\Delta QNR \cong \Delta MNR$ by HL

Question 62

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Objective: Identify the triangle congruency theorem that can be used to prove two triangles congruent.

Which congruence theorem can be used to prove $\triangle WXS \cong \triangle YZS?$



Question 63

Objective: Identify the triangle congruency theorem that can be used to prove two triangles congruent.

Two sides and the non-included right angle of one right triangle are congruent to the corresponding parts of another right triangle. Which congruence theorem can be used to prove that the triangles are congruent?



C _{SSS}

 \bigcirc

SAS HL

Question 64

Objective: Complete the steps to prove angles, segments, and triangles are congruent using triangle congruence theorems and CPCTC.

The proof that $HG \cong EG$ is shown.

Given: G is the midpoint of KF

KH || EF

Prove: $HG \cong EG$



What is the missing reason in the proof?

Statement	Reason
1. ∠EGF ≅ ∠HGK	1. vert. ∠s are ≅
2. KH EF	2. given
$3. \angle F \cong \angle K$	3. alt. int. ∠s are ≅
4. G is the midpoint of KF	4. given
5. FG ≅ KG	5. def. of midpt.
6. ∆FEG ≅ ∆KHG	6. ?



Objective: Identify the parts that can be used to prove triangle congruency using SSS or HL.



Could ΔJKL be congruent to ΔXYZ ? Explain.

• Yes, if $JL \cong XZ$.

0

0

Yes, if XZ = 10.

No, because the hypotenuse of one triangle is equal in length to the leg of the other triangle.

No, because the leg of one triangle is equal in length to the leg of the other triangle.

Question 66

Objective: Complete the steps to prove triangles are congruent using SSS or HL.

The proof that $\triangle QPT \cong \triangle QRT$ is shown.

Given: $SP \cong SR$ Prove: $\triangle QPT \cong \triangle QRT$


What is the missing reason in the proof?

Statements	Reasons
1. SP ≅ SR	1. given
2. ST ⊥ PR	2. converse of the perpendicular bisector theorem
3. PT ≅ RT	3. ?
4. QT ⊥ PR	4. ST and QT name the same line.
5. QP ≅ QR	5. perpendicular bisector theorem
6. $\Delta QPT \cong \Delta QRT$	6. HL theorem

definition of perpendicular bisector

- C definition of congruence
- C reflexive property

 \bigcirc

substitution property

Question 67

Objective: Determine the isometric transformations that would map one triangle onto another triangle given that three corresponding sides are congruent.



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Triangle DEF is congruent to ^{\Delta}GHJ by the SSS theorem. Which rigid transformation is required to map ^{\Delta}DEF onto ^{\Delta}GHJ?
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C dilation

reflection

rotation translation

Question 68

Objective: Determine the isometric transformations that would map one triangle onto another triangle given that three corresponding sides are congruent.

The triangles are congruent by the SSS congruence theorem.



Question 69

Objective: Identify the side and angles that can be used to prove triangle congruency using ASA or AAS.

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O







What additional information is needed to prove that the triangles are congruent using the AAS congruence theorem?

$$\begin{array}{c} \mathsf{C} \quad \mathsf{LO} \cong \mathsf{LM} \\ \bullet \quad \mathsf{OA} \cong \mathsf{MA} \\ \checkmark_{\mathsf{LOA}} \cong \checkmark_{\mathsf{LMA}} \\ \bullet \quad \circlearrowright_{\mathsf{LAO}} \cong \checkmark_{\mathsf{LAM}} \end{array}$$

<u>Question 71</u> Objective: Complete the steps to prove triangles are congruent using ASA or AAS.

The proof that ${}^{\bigtriangleup}\mathsf{MNG}\cong{}^{\bigtriangleup}\mathsf{KJG}$ is shown.



What is the missing reason in the proof?

	Statement		Reason
1.	NG ≅ JG	1.	given
2.	∠N and ∠J are right angles	2.	given
3.	∠MGN ≅ ∠KGJ	3.	vert. ∠s are ≅
4.	∠N≅∠J	4.	rt. ∠s are ≅
5.	∆MNG ≅ ∆KJG	5.	?
		•	
the reflexive proper	ÿ		

O AAS

ASA

O

O

the third angle theorem

Question 72

Objective: Determine the isometric transformations that would map one triangle onto another triangle given that two pairs of corresponding angles and one pair of corresponding sides are congruent.



Two rigid transformations are used to map $^{\triangle}$ ABC to $^{\triangle}$ QRS. The first is a translation of vertex B to vertex R. What is the second transformation?

o a reflection across the line containing AB

- 0
 - a rotation about point B
- C a reflection across the line containing CB
- C a rotation about point C

Objective: Determine the isometric transformations that would map one triangle onto another triangle given that two corresponding sides and the included angle are congruent.



Is there a series of rigid transformations that could map ΔQRS to ΔABC ? If so, which transformations could be used?

No, Δ QRS and Δ ABC are congruent but Δ QRS cannot be mapped to Δ ABC using a series rigid transformations.

No, \triangle QRS and \triangle ABC are not congruent.

Yes, Δ QRS can be translated so that R is mapped to B and then rotated so that S is mapped to C. Yes, Δ QRS can be translated so that Q is mapped to A and then reflected across the line containing QS.

Question 74

0

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 \mathbf{O}

Objective: Determine the isometric transformations that would map one triangle onto another triangle given that two corresponding sides and the included angle are congruent.



How can a translation and a reflection be used to map Δ HJK to Δ LMN?

- Translate K to N and reflect across the line containing HJ. Translate K to N and reflect across the line containing JK.
- C Translate H to L and reflect across the line containing JK.

C Translate K to L and reflect across the line containing HJ.

Question 75

Objective: Identify the sides and angle that can be used to prove triangle congruency using SAS.



In the diagram, $\angle J \cong \angle M$ and $\boxed{JL} \cong \boxed{MR}$. What additional information is needed to show $\triangle JKL \cong \triangle MNR$ by SAS?

$$\begin{array}{c} C \\ KL \cong NR \\ C \\ \angle L \cong \angle R \\ C \\ \angle K \cong \angle N \end{array}$$

 $\mathsf{JK}\cong\mathsf{MN}$

Question 76

Objective: Identify the sides and angle that can be used to prove triangle congruency using SAS.

Which pair of triangles can be proven congruent by SAS?





In which figure is point G a centroid?







In the diagram, which **must** be true for point D to be an orthocenter?

- BE, CF, and AG are angle bisectors. BE \perp AC, AG \perp BC, and CF \perp AB.
- C BE bisects AC, CF bisects AB, and AG bisects BC.

^C BE is a perpendicular bisector of AC, CF is a perpendicular bisector of AB, and AG is a perpendicular bisector of BC.

Question 79

Objective: Solve for unknown measures created by medians in a triangle.



In triangle TRS, VZ = 6 inches. What is RZ?

C 3 inches

О

- 6 inches 12 inches
- C 18 inches

Question 80 Objective: Solve for unknown measures created by medians in a triangle.



What is the length of segment NS?

C 1 unit

C 2 units 4 units

C 6 units

<u>Question 81</u> Objective: Identify characteristics of an isosceles triangle.

Triangle KNM is shown.



What is true about the sides of KNM?

$$KN = NM$$

$$KN + NM = KM$$

$$KM = 2(NM)$$

$$KN = \frac{1}{2}KM$$

<u>Question 82</u> Objective: Identify characteristics of an isosceles triangle.

Triangle XYZ is isosceles. Angle Y measures a°.



What expression represents the measure of angle X?



Question 83

Objective: Solve for unknown measures of isosceles triangles.

Triangle JKL is isosceles. The measure of angle J is 72° and the measure of angle K is 36°. Which statement describes angle L?

- Angle L is a base angle and measures 36°. Angle L is a base angle and measures 72°.
- C Angle L is a vertex angle and measures 36°.
- C Angle L is a vertex angle and measures 72°.

Question 84

Objective: Solve for unknown measures of isosceles triangles.

A regular pentagon is created using the bases of five congruent isosceles triangles, joined at a common vertex.



The total number of degrees in the center is 360°. If all five vertex angles meeting at the center are congruent, what is the measure of a base angle of one of the triangles?



C 108°

O

144°

<u>Question 85</u> Objective: Identify angle and side relationships in a triangle.

Consider triangle WXY.



Which statement about the angles is true?

Angle W is greater than angle Y.

- Angle Y is the largest angle.
- C Angle X is smaller than angle W.
- Angle W is the smallest angle.

<u>Question 86</u> Objective: Identify angle and side relationships in a triangle.

The lengths of the sides of triangle XYZ are written in terms of the variable *m*, where $m \ge 6$.



Which is correct regarding the angles of the triangle?



Question 87

Objective: Identify angle and side relationships between two triangles.



Objective: Solve real world problems involving relationships between angle measures and side lengths of one or two triangles.

Nigel and Mia are searching for a treasure chest under water. The straight line distance between them is 100 meters.



Given the angles in the diagram, who is closer to the treasure chest and why?

Nigel is closer because his distance to the chest is opposite the larger angle. Mia is closer because her distance to the chest is opposite the smaller angle.

^C Nigel is closer because his distance from the chest is 100 meters.

^C Mia is closer because her distance from the chest is 100 meters.

Question 89

Objective: Analyze the relationships between the angles of acute, right, and obtuse triangles.

If triangle RST is an acute triangle, then $m \angle S$ **must** be

less than 90°.

- C equal to 90°.
- equal to 100°.
- ^C greater than 90° and less than 180°.

Question 90

Objective: Analyze the relationships between the angles of acute, right, and obtuse triangles.

If isosceles triangle ABC has a 130° angle at vertex B, which statement must be true?

° "

m∠A = 15° and *m*∠C = 35° *m*∠A + *m*∠B = 155°

C m∠A + m∠C = 60°

 $^{\circ}$ $m \angle A = 20^{\circ}$ and $m \angle C = 30^{\circ}$

Question 91

Objective: Determine the length or parameters for a third side of a triangle given the other two sides.



Based on the diagram, which expresses all possible lengths of segment AB?



Question 92

Objective: Determine the length or parameters for a third side of a triangle given the other two sides.

Chang knows one side of a triangle is 13 cm. Which set of two sides is possible for the lengths of the other two sides of this triangle?

^C 5 cm and 8 cm

6 cm and 7 cm

O

O

7 cm and 2 cm 8 cm and 8 cm

Question 93

Objective: Identify and relate the interior and exterior angles of a triangle.



Which angle is an adjacent interior angle to ∠JKM?

C ZJKL ZMKL C ZKLM C ZLMK

Question 94

Objective: Identify and relate the interior and exterior angles of a triangle.



Which statements regarding the diagram of \triangle EBC are true? Select **three** options.

 \square \angle BEC is an exterior angle.

∠DEC is an exterior angle.

 $\angle ABE$ and $\angle EBC$ are supplementary angles.

 \angle BCF and \angle DEC are supplementary angles.

 \angle BEC is a remote interior angle to exterior \angle BCF.

Question 95

 \Box

Objective: Calculate the measures of interior and exterior angles of a triangle.



What is *m*∠ABC?

- C *m*∠ABC = 15°
- $m \angle ABC = 45^{\circ}$ $m \angle ABC = 60^{\circ}$
- \square m∠ABC = 75°

<u>Question 96</u> Objective: Calculate the measures of interior and exterior angles of a triangle.



What is the value of x?



Question 97

Objective: Write the equation of a line parallel to a given line that goes through a particular point.



What is the equation of the line that is parallel to the given line and passes through the point (-2, 2)?



Question 98 Objective: Write the equation of a line parallel to a given line that goes through a particular point.

The given line passes through the points (0, -3) and (2, 3). y 3 (2, 3)



What is the equation, in point-slope form, of the line that is parallel to the given line and passes through the point $(^{-1, -1})$?

 $\bigcirc y+1 = -3(x+1)$

$$y+1 = -\frac{1}{3}(x+1)$$

$$C \quad \begin{array}{c} y + 1 = \frac{1}{3}(x+1) \\ y + 1 = 3(x+1) \end{array}$$

Question 99

Objective: Write the equation of a line perpendicular to a given line or segment that goes through a particular point.

The given line segment has a midpoint at (3, 1).



What is the equation, in slope-intercept form, of the perpendicular bisector of the given line segment?



Question 100

Objective: Write the equation of a line perpendicular to a given line or segment that goes through a particular point.

A given line has the equation 2x + 12y = -1.

What is the equation, in slope-intercept form, of the line that is perpendicular to the given line and passes through the point (0, 9)?

$$C = \frac{y = \frac{1}{6}x + 9}{y = 6x + 9}$$

Question 101

Objective: Determine if two lines are parallel or perpendicular.



Which statement best explains the relationship between lines FG and HJ?

0

 \bigcirc

They are perpendicular because their slopes are equal.

They are perpendicular because their slopes are negative reciprocals.

They are not perpendicular because their slopes are equal. They are not perpendicular because their slopes are not negative reciprocals.

Question 102

Objective: Determine if two lines are parallel or perpendicular.



Which statement best explains the relationship between lines CD and FG?

- C They are perpendicular because their slopes are equal. They are perpendicular because their slopes are negative reciprocals.
- C They are not perpendicular because their slopes are equal.

They are not perpendicular because their slopes are negative reciprocals.

Question 103

 \bigcirc

Objective: Use slope criteria to find additional points on a line parallel or perpendicular to a given line.



Which point on the y-axis lies on the line that passes through point G and is parallel to line DF?



<u>Question 104</u> Objective: Use slope criteria to find additional points on a line parallel or perpendicular to a given line.



Which point is on the line that passes through point Z and is perpendicular to line AB?

(-4, 1)

- C (1, −2)
- C (2, 0)
- C (4, 4)

Question 105

Objective: Apply theorems to determine if lines are parallel.

Which diagram shows lines that must be parallel lines cut by a transversal?





Question 106 Objective: Apply theorems to determine if lines are parallel.

Lines **a** and **b** are parallel lines cut by transversal *f*.



Question 107 Objective: Apply theorems to determine if lines are parallel.



If $a \parallel b$ and $e \parallel f$, what is the value of y?



Question 108

Objective: Prove lines are parallel given angle relationships.

Given: $\boxed{\frac{NM}{LM} \parallel \overline{PO}}_{LM}$ and $\angle 1 \cong \angle 3$ Prove:



Statements	Reasons		
1. NM∥PO	1. given		
2. ∠2≅∠3	2. alternate interior angles theorem		
3. ∠1≅∠3	3. given		
4. ∠1≅∠2	4. ?		
5. IM∥NO	5. converse of alternate interior angles theorem		

What is the missing reason in the proof?

C given transitive property

C alternate interior angles theorem

converse alternate interior angles theorem

Question 109

 \bigcirc

Objective: Solve for angle measures when parallel lines are cut by a transversal.

Two parallel lines are crossed by a transversal.



What is the value of y?

C y = 40 y = 80

$$\begin{array}{c} \mathbf{C} \\ \mathbf{y} = 100 \\ \mathbf{C} \\ \mathbf{y} = 120 \end{array}$$

Objective: Solve for angle measures when parallel lines are cut by a transversal.

Two parallel lines are crossed by a transversal.



What is the value of *d*?

 $\begin{array}{c} C \\ d = 55 \\ C \\ d = 75 \\ d = 125 \\ C \\ d = 155 \end{array}$

Question 111

Objective: Solve for angle measures when parallel lines are cut by a transversal.

A pipe cleaner lay across a wire shelf. The wires that make up the shelf are parallel, and the pipe cleaner is a transversal. The parallel wires are labeled *a*, *b*, and, *c*, and the angles are labeled with numbers.



The measure of one angle is 130°. Which statement is true regarding the 130° angle and angle 3?

- C They are same-side interior angles, so angle 3 measures 50°. They are alternate interior angles, so angle 3 also measures 130°.
- C They are corresponding angles, so angle 3 also measures 130°.
- C They are alternate exterior angles, so angle 3 measures 50°

Objective: Complete the steps to prove angle relationships given parallel lines cut by a transversal.

Consider the diagram. $\begin{array}{c}
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Question 113

Objective: Identify parallel, perpendicular, and skew lines from three-dimensional figures.

Consider the diagram.



Lines e and c can be described as

- C intersecting.
- C parallel.

O

perpendicular. skew.

Question 114

Objective: Identify parallel, perpendicular, and skew lines from three-dimensional figures.

Planes X and Y are perpendicular. Points A, E, F, and G are points only in plane X. Points R and S are points in both planes X and Y. Lines EA and FG are parallel.



Based on this information, which pair of lines, together, could be perpendicular to RS? Select **two** options.

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Objective: Solve problems involving the distance from a point on the perpendicular bisector to both endpoints of the line segment.

In the diagram, CE=12 units and BE=5 units.



Based on the given information, what is AE?

\cap		
€.	2	units

 \mathbf{O}

7 units 12 units

C 17 units

Question 116

Objective: Solve problems involving the distance from a point on the perpendicular bisector to both endpoints of the line segment.

In the diagram, the length of segment QV is 15 units.



What is the length of segment TQ?

C 4 units

O

 \bigcirc

11 units 14 units

15 units

Question 117

Objective: Identify reflectional symmetry in geometric figures and the number of lines of symmetry.

The figure is an isosceles trapezoid.



How many lines of reflectional symmetry does the trapezoid have?



Question 118

Objective: Identify reflectional symmetry in geometric figures and the number of lines of symmetry.



Which statements are true about the reflectional symmetry of a regular heptagon? Select two options.

Lt has only 1 line of reflectional symmetry.

A line of symmetry will connect 2 vertices.

A line of symmetry will connect a vertex and a midpoint of an opposite side.

It has 7-fold symmetry.

A line of symmetry will connect the midpoints of 2 opposite sides.

<u>Question 119</u> Objective: Identify rotational symmetry and its order in geometric figures.



At which angle will the hexagon rotate onto itself?

C 60°

C 90°

O

120° 180°

<u>Question 120</u> Objective: Identify rotational symmetry and its order in geometric figures. A clock is constructed using a regular polygon with 60 sides. The polygon rotates every minute. How much has the polygon rotated after 7 minutes?



Question 121

Objective: Determine the image or pre-image of a figure after a given rotation.



Triangle ABC is shown on the graph. What are the coordinates of the image of point B after the triangle is rotated 270° about the origin?

(4, 2)

° (2, 4)

Question 122

Objective: Determine the image or pre-image of a figure after a given rotation.

A rectangle is transformed according to the rule $R_{0,00^{\circ}}$. The image of the rectangle has vertices located at R'(-4, 4), S'(-4, 1), P'(-3, 1), and Q'(-3, 4). What is the location of Q?

 $\begin{array}{c}
\mathbf{C} & (-4, -3) \\
\mathbf{C} & (-3, -4) \\
\mathbf{C} & (3, 4) \\
(4, 3)
\end{array}$

Question 123

Objective: Describe the properties of and write rules for rotations.

A parallelogram is transformed according to the rule $(x, y) \rightarrow (x, y)$. Which is another way to state the transformation?



C R0, 180°

C R0, 270° R0, 360

Question 124

Objective: Describe the properties of and write rules for rotations.

Triangle ABC is rotated to create the image A'B'C'.



Which rule describes the transformation?

$$C (x, y) \rightarrow (x, -y)$$

$$C (x, y) \rightarrow (y, x)$$

$$(x, y) \rightarrow (-x, -y)$$

$$C (x, y) \rightarrow (-y, -x)$$

Objective: Write the rule that describes a given translation.

The function rule $T_{-4, 6}(x, y)$ could be used to describe which translation?

a parallelogram on a coordinate plane that is translated 4 units down and 6 units to the right a trapezoid on a coordinate plane that is translated 4 units to the left and 6 units up

C a rhombus on a coordinate plane that is translated 4 units down and 6 units to the left

a rectangle on a coordinate plane that is translated 4 units to the right and 6 units up

Question 126

О

Objective: Write the rule that describes a given translation.

Right triangle LMN has vertices L(7, -3), M(7, -8), and

N(10, -8). The triangle is translated on the coordinate plane so the coordinates of L' are (-1, 8).

Which rule was used to translate the image?

C
$$(x, y) \rightarrow (x + 6, y - 5)$$

C $(x, y) \rightarrow (x - 6, y + 5)$
C $(x, y) \rightarrow (x + 8, y - 11)$
 $(x, y) \rightarrow (x - 8, y + 11)$

Question 127

Objective: Determine the image or pre-image of a figure after a given translation.

```
Triangle PQR has vertices

rule (x, y) \rightarrow (x - 2, y - 16)

What is the y-value of P'?

-18

-16

-12

-10
```

Question 128

Objective: Determine the image or pre-image of a figure after a given translation.



Square RSTU is translated to form R'S'T'U', which has vertices R'(-8, 1), S'(-4, 1), T'(-4, -3), and U'(-8, -3). If point S has coordinates of (3, -5), which point lies on a side of the pre-image, square RSTU?

 $\begin{array}{c} C \\ (-5, -3) \\ C \\ (3, -3) \\ (-1, -6) \\ C \\ (4, -9) \end{array}$

Question 129

Objective: Describe the properties of and write rules for reflections.

The image of trapezoid PQRS after a reflection across is trap

is trapezoid P'Q'R'S'.

₩Ŷ



Objective: Describe the properties of and write rules for reflections.

A line segment has endpoints at (-1, 4) and (4, 1). Which reflection will produce an image with endpoints at (-4, 1) and (-1, -4)?

```
C a reflection of the line segment across the x-axis
```

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C a reflection of the line segment across the y-axis
```

C a reflection of the line segment across the line y = x a reflection of the line segment across the line y = -x

Question 131

Objective: Determine the image or pre-image of a figure after a given reflection.


What are the coordinates of the image of vertex F after a reflection across the line y = -x?



Question 132

Objective: Determine the image or pre-image of a figure after a given reflection.



Which figure represents the image of parallelogram LMNP after a reflection across the line y = x?



 \mathbf{O} figure B figure C

O figure D

Objective: Determine if a transformation is isometric and identify corresponding parts of the pre-image and image.



Which statement about the transformation is true?

It is rigid because all side lengths and angles are congruent.

- C It is rigid because no side lengths or angles are congruent.
- C It is nonrigid because all side lengths are congruent.
- C It is nonrigid because no side lengths or angles are congruent.

Question 134

Objective: Determine if a transformation is isometric and identify corresponding parts of the pre-image and image.

All side lengths in quadrilateral PQRS measure 4 units. A transformation maps PQRS to P'Q'R'S'. All sides of P'Q'R'S' measure 1 unit.

Is the transformation an isometric transformation? Explain.

- ^C Yes, the side lengths in the two figures are proportional.
 - Yes, one figure maps to the other. No, the side lengths are not preserved.

No, the angles are not preserved.

Question 135

0

O

Objective: Identify the type of transformation given a pre-image and an image.



Which transformation maps the large triangle onto the small triangle?

dilation

C reflection

C rotation

C translation

Question 136

Objective: Identify the type of transformation given a pre-image and an image.

A transformation of Δ KLM results in Δ K'L'M'.



Which transformation maps the pre-image to the image?

dilation

C translation

C reflection

C rotation

Question 137

Objective: Identify complementary angles and supplementary angles from given diagrams.

Line JM intersects line GK at point N.



Which statements are true about the figure? Select two options.

C_{GNJ} is complementary to [∠]JNK.
 [∠]MNL is complementary to [∠]KNL.
 [∠]MNG is complementary to [∠]GNJ.
 [∠]KNJ is supplementary to [∠]MNL.
 [∠]GNM is supplementary to [∠]JNK.

Question 138

Objective: Identify complementary angles and supplementary angles from given diagrams.

Two parallel lines are intersected by a third line so that angles 1 and 5 are congruent.



Which statement is true about angles 3 and 5?

0	They	are	acute
	тпеу	are	acute.

- C They are congruent.
- C They are complementary. They are supplementary.

<u>Question 139</u> Objective: Solve problems involving measures of complementary and supplementary angles.

Angle RST is a right angle. Angle RSU has a measure of 25°.



What is the measure of angle TSU?



Question 140

Objective: Complete the steps to prove statements using complementary angles and supplementary angles.



Which reason justifies the statement that $^{\angle}$ KLC is complementary to $^{\angle}$ KJC?

Angles that are congruent are complementary to the same angle.

- C Angles that are congruent are supplementary to the same angle.
- C All angles in a rectangle are right angles.
- C Complementary angles are always also congruent.

Question 141 Objective: Identify linear pairs and vertical angles from given diagrams.

In which diagram do angles 1 and 2 form a linear pair?



Question 142 Objective: Calculate angle measures by using definitions and theorems about linear pairs and vertical angles.

In the diagram, what is m^2 VSR?





Objective: Calculate angle measures by using definitions and theorems about linear pairs and vertical angles.



Question 144 Objective: Complete the steps to prove statements using linear pairs and vertical angles.

Given:
$$m^{\checkmark}$$
TRV = 60°
 m^{\checkmark} TRS = (4x)°

Prove: x = 30



What is the missing reason in step 3?

Statements	Reasons
1. $m \angle \text{TRV} = 60^\circ$; $m \angle \text{TRS} = (4x)^\circ$	1. given
∠TRS and ∠TRV are a linear pair	definition of linear pair
3. $m \angle \text{TRS} + m \angle \text{TRV} = 180$	3. ?
4. $60+4x = 180$	4. substitution property of equality
5. $4x = 120$	5. subtraction property of equality
6. $x = 30$	6. division property of equality

 \odot

substitution property of equality angle addition postulate

- Subtraction property of equality
- C addition property of equality

Question 145

Objective: Complete the steps to prove algebraic and geometric statements.

What is the missing reason in the proof?

Given: ∠ABC is a right angle, ∠DBC is a straight angle

Prove: $\angle ABC \cong \angle ABD$



Statements	Reasons
 ∠ABC is a right angle 	1. given
∠DBC is a straight angle	2. given
 m∠ABC=90° 	definition of right angle
 m∠DBC = 180° 	definition of straight angle
5. $m \angle ABD + m \angle ABC = m \angle DBC$	angle addition property
 m∠ABD + 90° = 180° 	6. substitution property
7. $m \angle ABD = 90^{\circ}$	subtraction property
8. ∠ABC ≅ ∠ABD	8. ?

0

O

definition of angle bisector

segment addition property definition of congruent angles

transitive property

Question 146

Objective: Identify proof formats, the essential parts of a proof, and the assumptions that can be made from a given drawing.

C B E F

Ē₿

Given that bisects ∠CEA, which statements must be true? Select **three** options.

m∠CEA = 90°

 $\square \qquad m \angle CEF = m \angle CEA + m \angle BEF$

 $\square m \angle CEB = 2(m \angle CEA)$

∠CEF is a straight angle.

∠AEF is a right angle.

Objective: Identify proof formats, the essential parts of a proof, and the assumptions that can be made from a given drawing.

The last step in a proof contains the	?	conclusion	
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Question 148

Objective: Identify proof formats, the essential parts of a proof, and the assumptions that can be made from a given drawing.

A flowchart proof

C contains a set of sentences explaining the steps needed to reach a conclusion.

uses inductive reasoning to prove a statement. uses a visual representation of the logical flow of steps needed to reach a conclusion.

Contains a table with a logical series of statements and reasons that reach a conclusion.

Question 149

Objective: Identify a midpoint or bisector of a line segment or angles.



Ray CE is the angle bisector of \checkmark ACD. Which statement about the figure must be true?



Question 150

Objective: Apply the ruler postulate and segment addition postulate to calculate the lengths of line segments.



If FG = 2 units, FI = 7 units, and HI = 1 unit, what is GH?

- C 3 units 4 units
- C 5 units
- C 6 units

Question 151

Objective: Apply the ruler postulate and segment addition postulate to calculate the lengths of line segments.

Point G lies between points F and H on \overline{FH} .



If the length of FH is 18 units, what is the value of x?

> <u>Question 152</u> Objective: Apply the protractor postulate and angle addition postulate to calculate angle measures.

Angle PSR measures 99°.



What is the measure	e of [—]	'PSQ i	in degre	es?

C 9° C 24° 45° C 54°

Question 153

Objective: Use undefined terms to precisely define parallel lines, perpendicular lines, ray, angle, arc, circle, and line segment.

Two lines	intersecting	at a	riaht	angle
1 100 11100	micorocounig	aru	ingine	angio

0

O

are parallel. are perpendicular.

form a ray.

form a line.

Question 154

Objective: Use undefined terms to precisely define parallel lines, perpendicular lines, ray, angle, arc, circle, and line segment.

Which figures can be precisely defined by using only undefined terms? Select **three** options.

angle	
arc	

circle

line segment

parallel lines

Objective: Identify and name a pair of parallel lines, a pair of perpendicular lines, a ray, an angle, an arc, a circle, and a line segment.



Which is the line shown in the figure?



C line WX

C line WZ

Question 156

Objective: Identify and name a pair of parallel lines, a pair of perpendicular lines, a ray, an angle, an arc, a circle, and a line segment.



Which rays are part of line BE?



Objective: Identify and name undefined terms of point, line, plane, and distance along a line.

Which undefined geometric term is described as an infinite set of points that has length but not width?

C plane

O

sphere

Question 158

Objective: Identify and name undefined terms of point, line, plane, and distance along a line.

Line segment AB measures 18 units.



What is *d*, the distance between tick marks on the number line?



O

2 units

- C 3 units
 - 9 units

Question 159

Objective: Identify and name undefined terms of point, line, plane, and distance along a line.

What is the distance between points A and B?



C −6 units

- C ⁻¹ units C _{5 units}
 - 6 units

Objective: Analyze descriptions and diagrams that illustrate basic postulates about points, lines, and planes.

The diagram shows several planes, lines, and points.



Which statement is true about line *h*?

- C Line *h* intersects line *f* at two points, A and B.
- C Line *h* is the intersection of planes \mathcal{R} and \mathcal{T} .
- C Line *h* intersects plane \mathcal{P} at point C. Line *h* has points on planes \mathcal{R} , \mathcal{P} , and \mathcal{T} .